# Universität Leipzig, Mathematisches Institut, Germany □ lorenzo.baldi@mis.mpg.de https://lorenzobaldi.github.io/ https://orcid.org/0000-0001-5601-0783

# Lorenzo Baldi

#### Research Interests

Real Algebra, Real Algebraic Geometry and their Applications, in particular:

- O Positive Polynomials
- Sums of Squares
- O Polynomial Optimization
- O Moment Problems

#### Current Position

1.6.2024 Humboldt Postdoctoral Fellow, Universität Leipzig, Algebra group Mentor: Rainer Sinn

#### Past Positions

- 1.1–31.5.'24 **Postdoctoral researcher**, Max Planck Institute for Mathematics in the Sciences, Nonlinear Algebra group
  - Mentor: Rainer Sinn
- 2022–2023 **Postdoctoral researcher**, Sorbonne University, PolSys team Mentors: Jérémy Berthomieu and Pierre Lairez

#### Education and Academic Habilitations

- 2024–2028 Qualification for *Maître de Conférences* positions, Section 25 (Mathematics), French academic habilitation for MdC (assistant professor)
- 2024–2028 Qualification for *Maître de Conférences* positions, Section 26 (Applied Math.), French academic habilitation for MdC (assistant professor)
- 2019–2022 **Ph. D. in Mathematics**, Inria Sophia Antipolis Université Côte d'Azur, ESR9 of POEMA network. Title: Effective Representations in Real Algebraic Geometry and Polynomial Optimization, Advisor: B. Mourrain Jury members: M-F. Roy (president), M. Laurent (reviewer), M. Schweighofer (reviewer), J-B. Lasserre, A. Parusiński and M. Putinar.
- 2017–2019 Master Degree in Mathematics, Università di Trento, 110/110 with honors, Title: Real Tensors and Algebraic Geometry.

  Supervisor: E. Ballico.
- 2014–2017 **Bachelor Degree in Mathematics**, *Università di Firenze*, 110/110 with honors, Title: Introduzione ai gruppi di movimenti rigidi. Supervisor: C. Casolo.

#### Grants and Academic Distinctions

- 2024–2026 **Humboldt Post-Doctoral Research Fellowship**, Universität Leipzig, awarded from the Alexander von Humboldt Foundation
  Mentor: Rainer Sinn
- 12.8–16.8.-24 IWOTA 2024, University of Kent, EMS Workshop funding
  - 30.10- Research School in Real Algebraic Geometry, SISSA, Trieste, Work-2.11.2023 shops funding
- 12-25.3.2023 Grant Oberwolfach Leibniz Graduate Students, Workshops funding
  - 2019–2022 **Ph. D. Scholarship in POEMA**, European Union's H2020 research and innovation programme, Marie Skłodowska-Curie Actions, grant n. 813211
  - 2017–2019 Path of Excellence for the Master in Mathematics, Università di Trento, including extra academic assignments and awarded on merit base
  - 2014–2017 Prize for the Bachelor in Mathematics and Computer Science, Università di Firenze, awarded to the four best Bachelor's students

## Engagement in the Research System

- 2024 Referee for SIAM Journal on Applied Algebra and Geometry; Numerical Algebra, Control and Optimization; Optimization Letters; Mathematics of Operations Research and International Symposium on Symbolic and Algebraic Computation
- 3.8.2024 Co-organizer of BM60, satellite event of MEGA 2024, Leipzig
  - 2023 Referee for Journal of Algebra and SIAM Journal on Optimization
  - 2023- Reviewer for zbMATH Open (Zentralblatt für Mathematik)
- 11.2.2022 Co-organizer of the POEMA ESR Day, in POEMA Workshop 4, online

#### Research works

#### **Preprints**

- [7] L. Baldi, G. Blekherman and R. Sinn, Nonnegative Polynomials and Moment Problems on Algebraic Curves. *Submitted preprint*. https://arxiv.org/abs/2407.06017
- [6] L. Baldi and B. Mourrain, Exact Moment Representation in Polynomial Optimization. Submitted Preprint.

https://arxiv.org/abs/2012.14652

#### Journal Publications

- [5] L. Baldi, B. Mourrain and A. Parusiński, On Łojasiewicz Inequalities and the Effective Putinar's Positivstellensatz. *Journal of Algebra*, 2024. https://doi.org/10.1016/j.jalgebra.2024.08.022
- [4] L. Baldi and L. Slot, Degree bounds for Putinar's Positivstellensatz on the hypercube. SIAM J. Appl. Algebra Geom., 2024, pp. 1–25. https://epubs.siam.org/doi/10.1137/23M1555430
- [3] L. Baldi and B. Mourrain, On the effective Putinar's Positivstellensatz and moment approximation. *Mathematical Programming* 200, 2023, pp. 71–103. https://doi.org/10.1007/s10107-022-01877-6

#### Conference Proceedings

[2] L. Baldi and B. Mourrain, Computing Real Radicals by Moment Optimization. *Proceedings of the 2021 on International Symposium on Symbolic and Algebraic Computation*. ISSAC '21. New York, NY, USA: Association for Computing Machinery, 2021, pp. 43–50. https://doi.org/10.1145/3452143.3465541

#### Thesis

[1] L. Baldi, Effective representations in real algebraic geometry and polynomial optimization. *Ph.D. Thesis*, 2022. https://theses.hal.science/tel-03937680

#### Selected Research Visits

- 10–12.7.2024 Università di Trento, TensorDec Laboratory
- 18–20.6.2024 Technical University of Dresden, Real Algebraic Geometry Group
  - 5–9.7.2023 Technical University of Dortmund, Algebra und Geometrie group
- 24–27.6.2023 Max Plank Institute Leipzig, Nonlinear Algebra group
- 19–23.6.2023 University of Magdeburg, Discrete, Convex and Toric Geometry group
- 8–10.6.2022 University of Konstanz, Research Group in Real Algebraic Geometry
- 30.5–3.6.'22 Max Plank Institute Leipzig, Nonlinear Algebra group

# Teaching Activity

- 2023 Lecturer (with S. Debus) for the Ph. D. course Semidefinite programming for Algebra, Geometry and Combinatorics, University of Magdeburg, 30h
- 2019 Informatica, tutorial exercises (teaching professor: R. Zunino), Department of Mathematics, Trento
- 2018 Geometria e algebra lineare, tutorial exercises (teaching professors: A. Bernardi and S. Siboni), Department of Civil, Environmental and Mechanical Engineering, Trento

## Programming Skills

Languages Julia, C, Singular, Magma, Maple, Macaulay2, Git, LATEX

Packages MomentTools.jl, PMO.jl, MultivariateSeries.jl developed

#### Selected Talks

- 10.13.2024 Nonnegative polynomials on algebraic curves, Summer School on Real Algebraic Geometry and Hodge Theory, Contributed, TU Dresden
- 13.8.2024 Truncated moment problems for genus one curves, *IWOTA*, invited minisymposium speaker, University of Kent
- 30.7.2024 Effective Positivstellensatz over the Rational Numbers for Finite Semialgebraic Sets, MEGA, contributed, Leipzig
- 11.7.2024 Carathéodory Numbers: a Real point of view on Nonnegative Decompositions, TensorDec Lab Seminar, invited, Università di Trento
- 25.6.2024 Nonnegative Polynomials and Moment Problems on Algebraic Curves, AROMATH seminar, invited, Inria Sophia Antipolis
- 18.6.2024 Nonnegative Polynomials and Moment Problems on Algebraic Curves, Geometry seminar, invited, TU Dresden
- 14.3.2024 Carathéodory numbers and flat extension for measures supported on genus one curves, Moments and Polynomials: Applications and Theory, contributed, Konstanz
- 8.2.2024 Carathéodory numbers for measures supported on genus one curves, Seminar on Nonlinear Algebra, invited, Leipzig
- 10.7.2023 The Cone of Nonnegative Forms on Genus One Curves, SIAM Conference on Applied Alg. Geom., invited minisymposium speaker, Eindhoven
- 6.7.2023 The Effective Putinar's Positivstellensatz on the Hypercube, Oberseminar Algebra und Geometrie, invited, TU Dortmund
- 22.6.2023 Non-negative Polynomials on Real Plane Curves, Math Oberseminar Universitat Magdeburg, invited, University of Magdeburg

- 16.6.2023 Complexity in Polynomial Optimization, Foundations of Computational Mathematics, invited workshop speaker, Paris
- 2.6.2023 Local Algebro-Geometric Properties for Complexity Estimates in Pol. Opt., SIAM Conf. on Opt., invited minisymposium speaker, Seattle
- 20.3.2023 Non-negative forms on cubic curves, New Directions in Real Algebraic Geometry, contributed, Oberwolfach
- 13.3.2023 Degree bounds for Putinar's Positivstellensatz on the hypercube, Real Algebraic Geometry with a View toward Koopman Operator Methods, contributed, Oberwolfach
- 25.7.2022 On Putinar's Positivstellensatz and Convergence Rates in Polynomial Opt., ICCOPT, invited minisymposium speaker, Lehigh University
- 24.6.2022 On Łojasiewicz Inequalities and the Effective Positivstellensatz, MEGA 2022, contributed, Krakow
- 10.6.2022 Convergence Rates and Flat Truncation in Lasserre's Hierarchies, seminar Reelle Geometrie und Algebra, invited, University of Konstanz
  - 1.6.2022 Flat Truncation in Polynomial Opt.: a Geometric and Algebraic Perspective, Seminar on Nonlinear Algebra, invited, MPI Leipzig
- 3.2.2022 On Finite Convergence and Convergence Rates in Polynomial Optimization, *Joint PolSys-SpecFun Seminar*, invited, online
- 16.12.2021 On Moment Approximation and the Effective Putinar's Positivstellensatz, POEMA Industrial Workshop, invited, INRIA
- 20.8.2021 Exact Moment Representation in Polynomial Optimization, SIAM Conference on Applied Alg. Geom., invited minisymposium speaker, online
- 20.7.2021 Computing real radicals by moment opt., ISSAC, contributed, online
- 10.6.2021 Exact Moment Representation in Polynomial Optimization, MEGA, contributed, online